



UNIVERSIDADE FEDERAL DO PARANÁ - UFPR  
CENTRO POLITÉCNICO  
DEPARTAMENTO DE MATEMÁTICA

# Seminários Contínuos do Programa de Pós-Graduação em Matemática

19 de outubro de 2018 - 15:30 - Anfiteatro A (Bloco PC)

## On the regularity of P.D.E.'s problems: connections with geometry, number theory, and Homer Simpson.

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**ABSTRACT.** In this seminar, we discuss some tools and techniques used to solve the following problem: let  $M$  be a closed smooth manifold,  $f$  a smooth function belonging to  $C^\infty(M)$  and  $L$  a linear partial differential operator. Let  $u$  be an element on a bigger and more general space  $D(M)$  that contains  $C^\infty(M)$ . Now, if  $u$  and  $f$  satisfy the equation

$$L(u) = f,$$

can we guarantee that  $u$  belongs to  $C^\infty(M)$ ?